

Algorithms and Data Structures

Summer Semester 2025

For discussion on Wednesday, June 18, 2025

1. (GTG Exercise C-9.27) Show how to implement the FIFO queue ADT using only a priority queue and one additional integer instance variable.
2. (GTG Exercise C-9.28) Professor Idle suggests the following solution to the previous problem. Whenever an item is inserted into the queue, it is assigned a key that is equal to the current size of the queue. Does such a strategy result in FIFO semantics? Prove that it is so or provide a counterexample.
3. (GTG Exercise R-10.21) The following implementation of binary search is used by GTG in their implementation of the `SortedTableMap` class:

```
1 def _find_index(self, k, low, high):
2     """Return index of the leftmost item with key greater than or equal
3         to k.
4
5         Return high + 1 if no such item qualifies.
6
7         That is, j will be returned such that:
8             all items of slice table[low:j] have key < k
9             all items of slice table[j:high+1] have key >= k
10        """
11     if high < low:
12         return high + 1 # no element
13                           qualifies
14     else:
15         mid = (low + high) // 2
16         if k == self._table[mid]._key:
17             return mid # found exact match
18         elif k < self._table[mid]._key:
19             return self._find_index(k, low, mid - 1) # Note: may return
20                                                         mid
21         else:
22             return self._find_index(k, mid + 1, high) # answer is right
23                                                         of mid
```

Consider the following variant of the find index method:

```

1 def _find_index(self, k, low, high):
2     if high < low:
3         return high + 1
4     else:
5         mid = (low + high) // 2
6         if self._table[mid].key < k:
7             return self._find_index(k, mid + 1, high)
8         else:
9             return self._find_index(k, low, mid - 1)

```

Does this always produce the same result as the original version? Justify your answer.

4. (GTG Exercise R-10.6) Which of the hash table collision-handling schemes could tolerate a load factor above 1 and which could not?
5. (GTG Exercise R-10.18) Explain why a hash table is not suited to implement a sorted map.
6. (GTG Exercise C-10.45) Describe how to modify a skip-list representation so that index-based operations, such as retrieving the item at index j , can be performed in $O(\log n)$ expected time.